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David T. Uminsky* (duminsky@math.ucla.edu), UCLA Mathematics Department, Los Angeles, CA 90095-1555, and Theodore Kolokolnikov, Hui Sun and Andrea Bertozzi. A theory of complex patterns arising from 2D particle interactions.

Pairwise particle interactions arise in diverse physical systems ranging from insect swarms to self assembly of nanoparticles. In this talk we will present a theory for the morphology of patterns in two dimensions - which can range from ring and annular states to more complex spot patterns with N-fold symmetry. Many of these patterns have been observed in nature although a general theory has been lacking, in particular how small changes to the interaction potential can lead to large changes in self-organized state. Emergence of these patterns is explained by a stability analysis of a ring solution. This analysis leads to analytic formulae involving the interaction potential that provide detailed information about the structure of complex equilibria. (Received September 17, 2010)