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Joseph Brennan, Department of Mathematics, University of Central Florida, Orlando, FL 32816, and **Guantao Chen*** (gchen@gsu.edu), Department of Mathematics and Statistics, Georgia State University, Atlanta, GA 30303. *Minimal Generators of cut-ideals of Graphs without K_4 -minors*. Preliminary report.

Let $G = (V, E)$ be a graph and \mathbb{K} be a field. We associate each edge-cut $[A, B]$ of G with a coordinate $q_{A|B}$ and each edge uv with two coordinates (s_{uv}, t_{uv}) . Let

$$\begin{aligned}\mathbb{K}[q] &:= \mathbb{K}[q_{A|B} \mid [A, B] \text{ is an edge-cut of } G] \\ \mathbb{K}[s, t] &:= \mathbb{K}[s_{uv}, t_{uv} \mid uv \in E] \quad \text{and} \\ \phi_G &: \mathbb{K} \mapsto \mathbb{K}[s, t], \quad q_{A|B} \mapsto \prod_{uv \in [A, B]} s_{uv} \prod_{xy \in E - [A, B]} t_{xy}.\end{aligned}$$

The kernel $I(G)$ of ϕ_G is called the cut-ideal of the graph G . Sturmfels and Sullivant conjectured that I_G is generated by quadrics if and only if G contains no K_4 -minor. We will address the recent progresses on this conjecture. (Received January 21, 2007)