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Dorothee D. Haroske* (haroske@minet.uni-jena.de), Mathematical Institute,
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Recently the concept of growth envelopes in function spaces was introduced. Basically, the idea is to measure unboundedness of functions that belong to Sobolev spaces W_p^k and more general scales of spaces. By Sobolev's famous embedding theorem it is known that for $k \leq n/p$, $1 \leq p < \infty$, there are (essentially) unbounded functions in W_p^k . Growth envelopes, consisting of a growth envelope function

$$\mathcal{E}_G^X(t) \sim \sup_{\|f\|_X \leq 1} f^*(t), \quad t > 0,$$

together with some additional fine index $u_G \in (0, \infty]$, proved to be a reasonable tool in order to characterise spaces.

In the past mainly local assertions, i.e. the behaviour of $\mathcal{E}_G^X(t)$ for small t , were considered. We recall some of the used proof methods for Sobolev spaces and briefly explain the ideas concerning spaces of Besov (and Triebel-Lizorkin) type. We present some global assertions and discuss phenomena connected with the above spaces and some weighted spaces, too.

Finally, we deal with Besov spaces defined on fractal h -sets. (Received November 28, 2005)