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**Qinglan Xia\*** (qlxia@math.ucdavis.edu), University of California at Davis, Department of Mathematics, One Shields Ave., Davis, CA 95616. *A variational problem related to optimal mass transportation and mud cracking.*

In this talk, I will present a variational model related to optimal mass transportation. It is motivated by the study of the formation of mud cracking. We study the regularity of the boundary of sets minimizing a quasi perimeter  $T(E) = P(E, \Omega) + G(E)$  with a volume constraint. Here  $\Omega$  is any open subset of  $\mathbb{R}^n$  with  $n \geq 2$ ,  $G$  is a lower semicontinuous function on sets of finite perimeter satisfying a condition that  $G(E) \leq G(F) + C|E \Delta F|^\beta$  among all sets of finite perimeter with equal volume. In the case of mud cracking,  $G$  is given by the Wasserstein distance from the varying sets to a given set. We show that under the condition  $\beta > 1 - \frac{1}{n}$ , any volume constrained minimizer  $E$  of the quasi perimeter  $T$  has both interior points and exterior points, and  $E$  is indeed a quasiminimizer of perimeter without the volume constraint. Using a well known regularity result about quasi minimizers of perimeter, we get the classical  $C^{1,\alpha}$  regularity for the reduced boundary of  $E$ . (Received February 04, 2006)