The Brocard-Ramanujan Diophantine equation

$$
x!+1=y^{2}
$$

is still an open problem. Many variants of the Brocard-Ramanujan Diophantine equation have been studied. In this talk, we will discuss the recent progress and the variants of the problem. (Received February 13, 2006)

