Luca Capogna, Scott Pauls and Jeremy T Tyson* (tyson@math.uiuc.edu), 1409 West Green Street, Urbana, IL 61801. Convexity and the horizontal second fundamental form for graphs in Carnot groups. Preliminary report.

Let \mathbb{G} be a Carnot (nilpotent stratified Lie) group. We characterize weakly convex functions (in the sense of Danielli-Garofalo-Nhieu or Lu-Manfredi-Stroffolini) in terms of positive definiteness of the horizontal second fundamental form of their graphs in $\mathbb{G} \times \mathbb{R}$. This is joint work with Luca Capogna and Scott Pauls. (Received February 14, 2006)