Jerrold R. Griggs* (griggs@math.sc.edu), Department of Mathematics, University of South Carolina, Columbia, SC 29212, and Gyula O.H. Katona, Rényi Institute of Mathematics, Hungarian Academy of Sciences, 13-15 Reáltanoda u., Budapest, 1053, Hungary. No four subsets forming an $N$. Preliminary report.
We are interested in the maximum size of a family $\mathcal{F}$ of subsets of the set $\{1,2, \ldots, n\}$, subject to the condition that a certain configuration is excluded. We survey results of this kind, and present new bounds on $|\mathcal{F}|$ for the case that $\mathcal{F}$ contains no four distinct subsets $A, B, C, D$ satisfying $A \subset C, A \subset D, B \subset C$. (Received January 04, 2007)

