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Vladimir Nikiforov* (vnikifrv@memphis.edu). *Spectral supersaturation in graphs*. Preliminary report.

Let G be a graph of order n and $\mu(G)$ be the largest eigenvalue of its adjacency matrix. A recent result states that if G is K_{r+1} -free, then $\mu(G) \leq \mu(T_r(n))$, where $T_r(n)$ is the r -partite Turán graph of order n .

It turns out that if $\mu(G) > \mu(T_r(n))$, then G has an unexpected wealth of subgraphs not present in $T_r(n)$. For instance, let $r = 2$ and $\mu(G) > \sqrt{\lfloor n^2/4 \rfloor} = \mu(T_2(n))$. Then G contains:

- (i) all odd cycles of length up to $\lceil c_1 n \rceil$;
- (ii) $\lceil c_2 n \rceil$ triangles sharing a common edge;
- (iii) a complete bipartite graph $K(\lceil c_3 \log n \rceil, \lceil c_3 \log n \rceil)$ with an edge in one of the parts. Here $c_1, c_2, c_3 > 0$ are independent of n .

Similar assertions hold for all $r > 2$.

These results are instances of spectral supersaturation in graphs; for average degree supersaturation was introduced by Erdős and Simonovits in 1983. (Received February 26, 2007)