

1077-05-190

**Korinne Dobosh\***, Department of Mathematics, Montclair State University, Montclair, NJ 07043, and **Samuel Kennedy**, School of Mathematical Sciences, Rochester Institute of Technology, Rochester, NY 14623. *Rank numbers of rook's graphs.*

A  $k$ -ranking of a graph  $G$  is a function  $f : V(G) \rightarrow \{1, 2, \dots, k\}$  such that if  $f(u) = f(v)$  then every  $u - v$  path contains a vertex  $w$  such that  $f(w) > f(u)$ . The rank number of  $G$ , denoted by  $\chi_r(G)$ , is the minimum  $k$  such that a  $k$ -ranking exists for  $G$ . Many papers have appeared in the topic of ranking, and several of them investigated the rank number of certain classes of Cartesian products. The rook's graph, denoted by  $K_n \times K_m$ , is the Cartesian product of complete graphs  $K_n$  and  $K_m$ . This graph represents the moves of a rook on an  $n \times m$  chess board. This graph contains a multitude of paths between any given vertices, and we must consider all paths between two vertices to ensure a labeling satisfies the ranking condition. We will discuss our results, including an explicit formula for  $\chi_r(K_n \times K_m)$  for certain  $m$ , as well as new bounds for  $\chi_r(K_n \times K_m)$  for all  $n$  and  $m$ , and results involving the structure of all minimal rankings of  $K_n \times K_m$ . (Received August 10, 2011)