1041-30-188 Michael T. Lacey (lacey@math.gatech.edu), School of Mathematics, Georgia Institute of Technology, Atlanta, GA 30332, T. Eric Sawyer (sawyer@mcmaster.ca), HH 311A ; Dept of Mathematics and Statistics, McMaster University, 1280 Main Street West, Hamilton, Ontario L8S 4K1, Canada, and Ignacio Uriarte-Tuero* (ignacio@math.msu.edu), Department of Mathematics, Michigan State University, East Lansing, MI 48824. Astala's conjecture on Hausdorff measure distortion under planar quasiconformal mappings.

In his celebrated paper on area distortion under planar quasiconformal maps (Acta 1994), Astala proved that a compact set E of Hausdorff dimension d is mapped under a K-quasiconformal map f to a set fE of Hausdorff dimension at most $d' = \frac{2Kd}{2+(K-1)d}$, and that this result is sharp. He conjectured (Question 4.4) that if the Hausdorff measure $\mathcal{H}^d(E) = 0$, then $\mathcal{H}^{d'}(fE) = 0$.

This conjecture was known to be true if d' = 0 (obvious), d' = 2 (Ahlfors), and d' = 1 (Astala, Clop, Mateu, Orobitg and UT, Duke 2008.) The approach in the last mentioned paper does not generalize to other dimensions.

Astala's conjecture was shown to be sharp in the class of all Hausdorff gauge functions in work of UT (IMRN, 2008).

Finally, we (the 3 named authors) jointly proved completely Astala's conjecture in all dimensions. The ingredients of the proof come from Astala's original approach, geometric measure theory, and some new weighted norm inequalities for Calderón-Zygmund singular integral operators which cannot be deduced from the classical Muckenhoupt A_p theory.

These results are intimately related to (not yet fully understood) removability problems for various classes of quasiregular maps.

The talk will be self-contained. (Received August 11, 2008)