1026-52-147 Erwin Lutwak and Deane Yang\* (dyang@poly.edu), Department of Mathematics, Polytechnic University, Six Metrotech Center, Brooklyn, NY 11201, and Gaoyong Zhang. Optimal Sobolev Norms and the Minkowski Problem.

The existence and uniqueness of an optimal  $L^p$  Sobolev norm for a function on  $\mathbb{R}^n$  is shown to be essentially equivalent to the existence and uniqueness of the solution to the  $L^p$  Minkowski problem for even measures. The former is established using the latter. This leads to new affine analytic inequalities, as well as a new proof of the affine  $L^p$  Sobolev inequality previously established by the authors. (Received February 24, 2007)