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Ya-Chen Chen* (ya-chen.chen@asu.edu), Sacramento, CA 95814. *Minimum $K(2,3)$ -Saturated Graphs.*

Let F be a graph. A graph is F -saturated if it has no F as a subgraph, but contains F after adding any new edge. The minimum number of edges in an F -saturated graph is $\text{sat}(n, F)$. An F -saturated graph on n vertices with $\text{sat}(n, F)$ edges is a $\text{sat}(n, F)$ -graph. Erdos, Hajnal, and Moon proved that the $\text{sat}(n, K(k))$ -graph is the join of $(n - k + 2)$ independent vertices to every vertex in a complete graph $K(k-2)$ on $(k-2)$ vertices.

Pikhurko obtained $\text{sat}(n, F)$ of the complete $(r+1)$ -partite graph $K(1, \dots, 1, t)$, as later did G. Chen, Faudree, and Gould. Let $K(2,3)$ be the complete bipartite graph whose partite sets have size 2 and 3. Pikhurko and Schmitt presented $K(2,3)$ -saturated graphs with $(2n - 3)$ edges and obtained a lower bound of $\text{sat}(n, K(2,3))$. Bohman, Fonoferova, and Pikhurko determined $\text{sat}(n, F)$ asymptotically for complete multipartite graph F as n tends to infinity and gave structural information about almost extremal F -saturated graphs. We prove their conjecture that $\text{sat}(n, K(2,3)) = 2n - 3$. (Received September 23, 2012)