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**Daniel W. Cranston, William B. Kinnersley, Suil O and Douglas B. West\***  
(west@math.uiuc.edu). *Game matching number of graphs.*

We study a competitive optimization version of  $\alpha'(G)$ , the maximum size of a matching in a graph  $G$ . Players alternate adding edges of  $G$  to a matching until it becomes a maximal matching. One player (Max) wants that matching to be large; the other (Min) wants it to be small. The resulting sizes under optimal play when Max or Min starts are denoted  $\alpha'_g(G)$  and  $\hat{\alpha}'_g(G)$ , respectively. We show that always  $|\alpha'_g(G) - \hat{\alpha}'_g(G)| \leq 1$ . We obtain a sufficient condition for  $\alpha'_g(G) = \alpha'(G)$  that is preserved under cartesian product. Always  $\alpha'_g(G) \geq \frac{2}{3}\alpha'(G)$ , with equality for many split graphs, while  $\alpha'_g(G) \geq \frac{3}{4}\alpha'(G)$  when  $G$  is a forest. Whenever  $G$  is a 3-regular  $n$ -vertex connected graph,  $\alpha'_g(G) \geq n/3$ , and such graphs exist with  $\alpha'_g(G) \leq 7n/18$ . For an  $n$ -vertex path or cycle, the value is roughly  $n/7$ . (Received September 23, 2012)