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Paul Pollack* (pollack@uga.edu), Boyd Graduate Studies Research Center, Mathematics Department, UGA, Athens, GA 30602. *The smallest prime with a given splitting type in an abelian number field.*

Let K/\mathbf{Q} be a finite, abelian extension. We describe a method, developed out of work of Linnik–Vinogradov and Elliott, for bounding above the smallest rational prime that is unramified and splits into a given number of distinct prime ideals in \mathcal{O}_K . One corollary is that for each $\epsilon > 0$, the smallest prime that splits completely in K is $O_{n,\epsilon}(|D|^{\frac{1}{4}+\epsilon})$, where n denotes the degree of K/\mathbf{Q} and D denotes its discriminant. We also give some applications to computing average prime-splitting statistics for families of number fields. (Received September 23, 2012)