1086-11-2892 Reyes Matiel Ortiz-Albino* (reyes.ortiz@upr.edu), 1011 Sonsire Chalets, Mayaguez, PR 00682. $\tau_{n}$-Number Theory. Preliminary report.

The study of a general theory of factorizations leads to the definition of a $\tau_{n}$-factorization or $\tau_{n}$-product, given by Anderson an Frazier, in 2006. They defined the concepts of $\tau_{n}$-irreducible elements, $\tau_{n}$-prime elements, and some properties of $\tau_{n}{ }^{-}$ factorizations. Later in 2007, Hamon characterized the $\tau_{n}$-atomicity of $\mathbb{Z}$, which only holds for $n=0,1,2,3,4,5,6,8$, 10 and 12. In 2008, Ortiz defined the greatest common $\tau_{n}$-divisor, unfortunately it does not always exists for an integer $n>1$. Nowadays, Ortiz has developed formulas to calculate a new type of ordered greatest common $\tau_{n}$-divisor and some arithmetic $\tau_{p}$-functions, where $p$ is a positive prime integer. Even though the $\tau_{n}$-gcd does not always exist, the ordered $\tau_{n}$-gcd is conjecture to always exist for any natural number $n$. (Received September 26, 2012)

