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**Alfred Geroldinger\*** ([alfred.geroldinger@uni-graz.at](mailto:alfred.geroldinger@uni-graz.at)), Institute for Mathematics and Scientific Comp, University of Graz, 8010 Graz, Austria. *Local and global tameness in Krull monoids.*

Let  $H$  be a Krull monoid with finite class group  $G$ , and let  $u \in H$  be an atom (an irreducible element). The local tame degree  $\mathfrak{t}(H, u)$  is the smallest integer  $N \in \mathbb{N}_0$  with the following property: for any multiple  $a$  of  $u$  and any factorization  $a = v_1 \cdot \dots \cdot v_n$  of  $a$  into atoms, there is a subproduct which is a multiple of  $u$ , say  $v_1 \cdot \dots \cdot v_m$ , and a refactorization of this subproduct which contains  $u$ , say  $v_1 \cdot \dots \cdot v_m = uu_2 \cdot \dots \cdot u_\ell$ , such that  $\max\{\ell, m\} \leq N$ .

The local tame degree  $\mathfrak{t}(H, u)$  measures the distance between an arbitrary factorization of  $a$  and a factorization of  $a$  which contains  $u$ . So  $u$  is a prime element iff  $\mathfrak{t}(H, u) = 0$ . The (global) tame degree  $\mathfrak{t}(H)$  is the supremum of the local tame degrees over all atoms  $u \in H$ . The finiteness of the class group easily implies that the finiteness of the tame degree.

We discuss upper and lower bounds for  $\mathfrak{t}(H)$ , and the relationship between  $\mathfrak{t}(H)$  and the tame degree  $\mathfrak{t}(\mathcal{B}(G))$ , where  $\mathcal{B}(G)$  is the monoid of zero-sum sequences over the class group  $G$ .

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