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Finding Formulas for the Complexity of Riemann Surfaces.

The *complexity* of a branched cover of a Riemann surface M to the Riemann sphere S^2 is defined as its degree times the hyperbolic area of the complement of its branching set in S^2 . The *complexity* of M is defined as the infimum of the complexities of all branched covers of M to S^2 . We prove that if M is a connected, closed, orientable Riemann surface of genus $g \geq 1$, then its complexity equals $2\pi(m_{\min} + 2g - 2)$, where m_{\min} is the minimum total length of a branch datum realizable by a branched cover $p: M \rightarrow S^2$. Also, we will explain why finding explicit formulas for the integer m_{\min} is a difficult problem that is related to the classical Hurwitz existence problem for branched covers of the Riemann sphere. (Received September 25, 2012)