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A pair of square 0, 1 matrices A, B such that $AB^T = E + kI$ (where E is the $n \times n$ matrix of all 1s and k is a positive integer) are called *Lehman matrices*. These matrices figure prominently in Lehman's seminal theorem on minimally nonideal matrices. There are two choices of k for which this matrix equation is known to have infinite families of solutions. When $n = k^2 + k + 1$ and A = B, we get point-line incidence matrices of finite projective planes, which have been widely studied in the literature. The other case occurs when k = 1 and n is arbitrary, but very little is known in this case. This talk discusses this class of Lehman matrices and classifies them according to their similarity to circulant matrices. (Received January 25, 2008)