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Ilya Kapovich\* (kapovich@math.uiuc.edu), UIUC Department of Mathematics, 1801 West Green Street, Urbana, IL 61801, and Martin Lustig (Martin.Lustig@univ-cezanne.fr), , France. Geometric Intersection Number and analogues of the Curve Complex for free groups.

For the free group  $F_N$  of finite rank  $N \ge 2$  we construct a canonical Bonahon-type continuous and  $Out(F_N)$ -invariant geometric intersection form

$$\langle , \rangle : \overline{cv}(F_N) \times Curr(F_N) \to \mathbb{R}_{\geq 0}$$

Here  $\overline{cv}(F_N)$  is the closure of unprojectivized Culler-Vogtmann's Outer space  $cv(F_N)$  in the equivariant Gromov-Hausdorff convergence topology (or, equivalently, in the length function topology). It is known that  $\overline{cv}(F_N)$  consists of all very small minimal isometric actions of  $F_N$  on  $\mathbb{R}$ -trees. The projectivization of  $\overline{cv}(F_N)$  provides a free group analogue of Thurston's compactification of the Teichmüller space. As an application, using the *intersection graph* determined by the intersection form, we show that several natural analogues of the curve complex in the free group context have infinite diameter. (Received January 18, 2008)