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Let $m^*(r, k)$ be the smallest number of edges in an r-uniform (k + 1)-chromatic simple hypergraph. Erdős and Lovász proved that

$$\frac{k^{2(r-2)}}{16r(r-1)^2} \le m^*(r,k) \le 1600r^4k^{2(r+1)}.$$

A result of Z. Szabó improves the lower bound by a factor of $r^{2-\epsilon}$. Elaborating ideas of Szabó, we improve the lower bound by another factor of r. (Received July 31, 2007)