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(ruanhj@math.cornell.edu), Department of Mathematics, Cornell University, Ithaca, NY 14853, and Robert S. Strichartz. The resolvent kernel for pcf self-similar fractals.

For the Laplacian Δ defined on a p.c.f. self-similar fractal, we give an explicit formula for the resolvent kernel of the Laplacian with Dirichlet boundary conditions. That is, we construct a symmetric function $G^{(\lambda)}$ which solves $(\lambda \mathbb{I} - \Delta)^{-1}f(x) = \int G^{(\lambda)}(x,y)f(y)d\mu(y)$. The method is similar to Kigami's construction of the Green kernel in Analysis on fractals, and is expressed as a sum of scaled and "translated" copies of a certain function $\psi^{(\lambda)}$ which may be considered as a fundamental solution of the resolvent equation. Examples of the explicit resolvent kernel formula are given for the unit interval, standard Sierpinski gasket, and the level-3 Siperpinski gasket SG_3 . (Received August 13, 2008)