1053-11-181
Xander Faber* (xander@math.mcgill.ca), McGill University, Department of Mathematics and Statistics, 805 Sherbrooke St. West, Montreal, Quebec H3A 2K6, Canada. Prime Factors of Dynamical Sequences.
Let $\phi(t) \in \mathbb{Q}(t)$ be a rational function of degree at least 2 . For a given rational number $x_{0}$, define $x_{n+1}=\phi\left(x_{n}\right)$ for each $n \geq 0$. If this sequence is not eventually periodic, then $x_{n+1}-x_{n}$ has a primitive prime factor for all sufficiently large $n$. This result provides a new proof of the infinitude of primes for each rational function $\phi$ of degree at least 2 .

I will present the above result, along with some interesting refinements. I will also give a geometric description that suggests a question about dynamics in higher dimensions. This is joint work with Andrew Granville. (Received September 02, 2009)

