Abstract: Fix a prime $p$ and let $X(p)$ be the modular curve over the integers classifying elliptic curves with full-level $p$ structure. The group $G:=\mathrm{SL}_{2}\left(\mathbf{F}_{p}\right)$ acts on $X(p)$ and hence on its (sheaf) cohomology. In this talk, we we will investigate the structure of the $\mathbf{Z}[G]$-module $M$ given by the global sections of the canonical sheaf. In particular, we will describe the reduction modulo $p$ of $M$ as a mod $p$ (modular) representations of $G$. This description relies heavily on the geometry of $X(p)$ in characteristic $p$ and uses Rosenlicht's description of the dualizing sheaf in terms of regular differential forms. (Received September 04, 2009)

