Sylvie Corteel and Carla D Savage* (savage@csc.ncsu.edu), Dept. of Computer Science, Box 8206, North Carolina State University, Raleigh, NC 27695-8206, and Andrew V Sills. A new view of the little Göllnitz products.
We give a combinatorial proof of the following theorem: The number of partitions of $N$ into distinct parts in which odd-indexed (even-indexed) parts are even is equal to the number of partitions of $N$ into parts congruent to $2,3,7$ (mod 8) $(1,5,6(\bmod 8))$. This provides a new view of the infinite products appearing in the little Göllnitz identities. We also show that a finite version of the little Göllnitz product counts lecture hall partitions in which in which odd-indexed (even-indexed) parts are even, giving an analog of the Lecture Hall Theorem of Bousquet-Mélou and Eriksson. (Received August 28, 2009)

