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**Jonathan D Browder\*** ([browder@math.washington.edu](mailto:browder@math.washington.edu)), 1620 N 45th St Apt 203, Seattle, WA 98103. *Face Numbers of Cohen-Macaulay Flag Complexes.*

A simplicial complex  $\Delta$  is *flag* if whenever  $\tau$  is a subset of the vertices of  $\Delta$  such that any two elements of  $\tau$  form an edge in  $\Delta$  then  $\tau$  is itself a face of  $\Delta$ . In other words, flag complexes are simplicial complexes that are completely determined by their edges. It was conjectured by Kalai and proved by Frohmader that if  $\Delta$  is a  $d$ -dimensional flag complex, then there is another  $d$ -dimensional simplicial complex,  $\Gamma$ , which has the same number of faces as  $\Delta$  in each dimension and is *balanced* (that is, properly  $d$ -colorable). Kalai further conjectured that if  $\Delta$  is in addition Cohen-Macaulay, we may take  $\Gamma$  to be Cohen-Macaulay as well.

In this talk I will exhibit a large class of complexes for which Kalai's conjecture holds, and explain the methods of the proof, which involves finding an appropriate isomorphic image of the Stanley-Reisner ring. I will also note how our class contains the class of Cohen-Macaulay complexes arising as independence complexes of graphs of sufficient girth. (Received January 17, 2011)