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**Konstantin I. Oskolkov\*** (kooskolkov@gmail.com), Department of Mathematics, University of South Carolina, Columbia, SC 29208. *On Riemann - Schrödinger function.*

Multi-fractal properties of the function

$$\Phi : \mathbb{R}^2 \mapsto \mathbb{C}, \quad \Phi(t, x) := \sum_{n \in \mathbb{Z} \setminus \{0\}} \frac{e^{\pi i (tn^2 + 2xn)}}{\pi i n^2}$$

will be discussed. It seems natural to name  $\Phi$  *Riemann - Schrödinger function* because: 1) the real part of the restriction of  $\Phi$  onto the line  $x = 0$  coincides with the famous function that was proposed by B. Riemann as *plausible* example of a continuous but nowhere differentiable function, and 2)  $\Phi$  is a generalized solution of the Schrödinger equation of a free particle,  $(4\pi i \partial_t - \partial_x^2)\Phi = 0$ . The properties of  $\Phi$ , particularly those of its' partial derivative  $\partial_x \Phi$  have implications in analytic number theory – all *incomplete Gauss' sums* are “encoded” in this derivative. (Received January 15, 2011)