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**William Green\***, 600 Lincoln Ave., Charleston, IL 61920. *Dispersive estimates for matrix and scalar Schrödinger operators in dimension five.*

We study the non-selfadjoint matrix Schrödinger operator

$$\mathcal{H} = \begin{bmatrix} -\Delta + \mu - V_1 & -V_2 \\ V_2 & \Delta - \mu + V_1 \end{bmatrix}$$

in dimension five. This operator arises when linearizing about standing wave solutions in certain non-linear partial differential equations. Here  $\mu > 0$  and  $V_1, V_2$  are real-valued decaying potentials. We examine the boundedness of the evolution operator  $e^{it\mathcal{H}}$  in the sense of  $L^1 \rightarrow L^\infty$ .

We prove  $L^1 \rightarrow L^\infty$  dispersive estimates for the matrix operator that are analogous to the known estimates for the evolution of the scalar Hamiltonian  $H = -\Delta + V$ . We show that if  $P_c$  is projection away from the eigenvalues of  $\mathcal{H}$ , along with standard assumptions on the spectrum of  $\mathcal{H}$ ,

$$\|e^{it\mathcal{H}}P_c\|_{1 \rightarrow \infty} \lesssim |t|^{-5/2}$$

holds with optimal assumptions on regularity of the potentials. We further discuss an improvement on the decay assumptions for the scalar case. (Received January 10, 2011)