

1068-42-209

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Let $0 < \beta < 1$, the Riesz Fractional Derivative of order β , is defined by

$$D_{\beta}^{\gamma} f = \frac{1}{c_{\beta}} \int_0^{\infty} t^{-\beta-1} (P_t - I) f dt,$$

and the Bessel Fractional Derivative by

$$\mathcal{D}_{\beta}^{\gamma} f = \frac{1}{c_{\beta}} \int_0^{\infty} t^{-\beta-1} (e^{-t} P_t - I) f dt,$$

where $c_{\beta} = \int_0^{\infty} u^{-\beta-1} (e^{-u} - 1) du < \infty$, since $0 < \beta < 1$.

For $\alpha \geq 0$, let k be the smallest integer greater than α and $1 \leq p, q < \infty$, the Gaussian Besov-Lipschitz space $B_{p,q}^{\alpha}(\gamma_d)$ is the set of functions $f \in L^p(\gamma_d)$ for which

$$\left(\int_0^{\infty} \left(t^{k-\alpha} \left\| \frac{\partial^k}{\partial t^k} P_t f \right\|_{p,\gamma_d} \right)^q \frac{dt}{t} \right)^{1/q} < \infty. \quad (1)$$

and the Gaussian Triebel-Lizorkin space $F_{p,q}^{\alpha}(\gamma_d)$ is defined analogously. In this talk, we will prove the next results:

Let $1 \leq p, q < +\infty$, $0 < \beta < \alpha < 1$ then D_{β}^{γ} and $\mathcal{D}_{\beta}^{\gamma}$ are bounded from $B_{p,q}^{\alpha}(\gamma_d)$ into $B_{p,q}^{\alpha-\beta}(\gamma_d)$ and also from $F_{p,q}^{\alpha}(\gamma_d)$ into $F_{p,q}^{\alpha-\beta}(\gamma_d)$. (Received January 18, 2011)