Stefaan De Winter, Department of Mathematics and Computer Algebr, Ghent University, 9000 Gent, Belgium, Felix Lazebnik* (lazebnik@math.udel.edu), Department of Mathematical Sciences, University of Delaware, Newark, DE 191716, and Jacques Verstraëte (jacques@ucsd.edu), Department of Mathematics, University of California, 9500 Gilman Drive, La Jolla, CA 92093-0112. An Extremal Characterization of Projective Planes.
We prove that amongst all $n$ by $n$ bipartite graphs of girth at least six, where $n=q^{2}+q+1 \geq 157$, the incidence graph of a projective plane of order $q$, when it exists, has the maximum number of cycles of length eight. This characterizes projective planes as the partial planes with the maximum number of quadrilaterals. (Received March 30, 2010)

