Eddie Cheng (echeng@oakland.edu), Dept. of Mathematics and Statistics, Oakland University, Rochester, MI 48309, Ke Qiu (kqiu@brocku.ca), Dept. of Computer Science, Brock University, St. Catharines, Ontario L2S 3A1, and Zhizhang Shen* (zshen@plymouth. edu), Dept. of Computer Science and Technology, Plymouth State Univestiy, Plymouth, NH 03264. The Number of Shortest Paths in the ( $n, k$ )-Star Graphs. Preliminary report.
Given a graph $G$, a well-known problem is to find the number of the shortest paths between a pair of vertices in $G$. A solution to this counting problem can serve as an important topological property for an interconnection network in terms of strong connectivity, effective fault-tolerance, lower communication cost and desired routing flexibility.

It turns out that the number of the shortest paths between $v$ and $e_{k}$ in an $(n, k)$-star graph equals the number of minimum factorizations of $v$ in terms of $(n, k)$-star transpositions, which we enumerate in this talk. (Received February 26, 2010)

