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Composition operators between subsets of function algebras.

This talk is based on a joint paper with E. Toneva. We expand the Banach-Stone theorem for non-linear isometries and also to non-unital function algebras. Let A and B be function algebras and A_1 be a dense subset of A . If $T: A_1 \rightarrow B$ is an isometry with a dense range, such that $\||Tf| + |Tg|\| = \||f| + |g|\|$ for all $f, g \in A$, and $T(ih_0) = i(Th_0)$, where $h_0 \in A_1$ does not vanish on the Choquet boundary δA of A , then T is a weighted composition operator on δB , i.e. there is a homeomorphism $\psi: \delta B \rightarrow \delta A$ and a continuous function $\alpha: \delta B \rightarrow \mathbb{C}$ so that $(Tf)(y) = \alpha(y) f(\psi(y))$ for all $f \in A_1$ and $y \in \delta B$. If, in addition, A_1 is an algebra, then so is $\bar{\alpha}T(A_1)$ and $\bar{\alpha} \cdot T: A_1 \rightarrow \bar{\alpha}T(A_1)$ is an isometric algebra isomorphism. We show also that if A and B are function algebras, A_1 is a dense subset of A and $T: A_1 \rightarrow B$ is an isometry with a dense range in B such that $\||Tf| + |Tg|\| = \||f| + |g|\|$ for all $f, g \in A_1$ and preserves the peripheral spectra, then δB is homeomorphic to δA and T is a composition operator on δB . (Received February 10, 2011)