1125-11-2334Paul Pollack* (pollack@uga.edu), Department of Mathematics, Boyd Graduate Studies
Research Center, University of Georgia, Athens, GA 30602. Torsion subgroups of CM elliptic
curves.

For each positive integer d, let T(d) denote the supremum of all orders of groups E(F)[tors] appearing for an elliptic curve E defined over a degree d number field F. A celebrated theorem of Merel asserts that $T(d) < \infty$ for all d. However, the known quantitative results in this direction are far from the conjectured truth. Let $T_{\text{CM}}(d)$ be defined the same way as T(d), but with the restriction to CM elliptic curves. I will discuss some recent statistical results concerning $T_{\text{CM}}(d)$ and related functions. Perhaps surprisingly, the "anatomy of integers" (as pioneered by Paul Erdős) plays a key role in the proofs. Joint work with Abbey Bourdon and Pete L. Clark. (Received September 20, 2016)