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Udita N. Katugampola* (udita@udel.edu), Department of Mathematical sciences, University of Delaware, Newark, DE 19716. *Can we generalize the limit-definition of the derivative?*

II. Preliminary report.

We consider the operator defined by

$$\mathcal{D}_\omega f(x) = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon \omega(x)) - f(x)}{\epsilon},$$

relative to a weight function ω , which acts as a **catalyst** and controls the convergence rate. Such a derivative obeys familiar properties such as the product rule, quotient rule, power rule, chain rule, Rolle's Theorem and Mean Value Theorems. It is interesting to note that the case of $\omega(x) = x^{1-\alpha}$, $\alpha \in \mathbb{R}$, is now known as the **conformable fractional derivative** though it lacks some key properties of a standard fractional derivative. Newly defined derivative is a close resemblance of several existing derivatives, namely, the directional derivative, the Fréchet and Gâteaux derivatives. We also define the corresponding weighted ω -integral in a weighted-space X_ω and discuss some properties related to differential equations governed by ω -derivatives. It is also interesting to observe that such an integral appears in several unrelated topics such as *Stochastic integrals*, the *Brunn-Minkowski theory*, *Wulff shapes*, *Bihari's inequality* and *Variational Calculus*. (Received September 20, 2016)