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Define the sequence  $\{b_n\}$  by  $b_0 = 1, b_1 = 2, b_2 = 1, b_3 = -3$ , and

$$b_n = \begin{cases} \frac{b_{n-1}b_{n-3}-b_{n-2}^2}{b_{n-4}} & \text{if } n \not\equiv 2 \pmod{3}, \\ \frac{b_{n-1}b_{n-3}-3b_{n-2}^2}{b_{n-4}} & \text{if } n \equiv 2 \pmod{3}. \end{cases}$$

We relate this sequence  $\{b_n\}$  to the coordinates of points on the elliptic curve  $E : y^2 + y = x^3 - 3x + 4$ . We use Galois representations attached to  $E$  to prove that the density of primes dividing a term in this sequence is equal to  $\frac{179}{336}$ . Furthermore, we describe an infinite family of elliptic curves whose Galois images match that of  $E$ . (Received August 06, 2015)