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Yeon June Kang*, yeonjunekang@gmail.com. *Triangulations via Iterated Largest Angle Bisection.*

For a given triangle $\triangle ABC$, with $\angle A \geq \angle B \geq \angle C$, the *largest angle bisection* procedure consists in constructing AD , the angle bisector of angle $\angle A$, and replacing $\triangle ABC$ by the two newly formed triangles, $\triangle ABD$ and $\triangle ACD$.

Let \triangle_{01} be a given triangle. Bisect \triangle_{01} into two triangles, \triangle_{11} and \triangle_{12} . Next, bisect each \triangle_{1i} , $i = 1, 2$, forming four new triangles \triangle_{2i} , $i = 1, 2, 3, 4$. Continue in this fashion. For every nonnegative integer n , $T_n = \{\triangle_{ni} : 1 \leq i \leq 2^n\}$, so T_n is the set of 2^n triangles created after the n -th iteration.

Define m_n , the *mesh* of T_n , as the length of the longest side among the sides of all triangles in T_n . Also, let γ_n be the smallest angle among the angles of the triangles in T_n . We prove the following results:

- $\gamma_n \geq \min(\gamma_0, 30^\circ)$.
- $m_n \rightarrow 0$ as $n \rightarrow \infty$.
- Unless \triangle_{01} is an isosceles right-angle triangle, the set $\bigcup_{n=0}^{\infty} T_n$ contains infinitely many triangles no two of which are similar.

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