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Neal Owen Bushaw* (neal@asu.edu) and **Nathan Kettle**. *Extremal Numbers for Forestable Graphs*.

The extremal number, $ex(n, G)$, of a graph G is the maximum number of edges among all G -free graphs of order n . Of considerable recent interest is the case when the forbidden graph is made up of several disjoint copies of some smaller graph. Equivalently, one can consider $ex(n, k \cdot G)$ - the maximum number of edges among all n vertex graphs not containing k vertex disjoint copies of G . The Erdős-Stone Theorem tells us that for a 3-chromatic (or higher) graph, the asymptotics for this are identical to the asymptotics for $ex(n, G)$. For bipartite graphs, however, $ex(n, G)$ and $ex(n, k \cdot G)$ can differ significantly, even in the limit.

Perhaps the most natural way to construct an order n graph which is kG -free is to take an extremal G -free graph of order $n - k + 1$, and join it to the complete graph K_{n-1} , adding all possible edges between the two. This graph is certainly $k \cdot G$ -free, as any copy of G must contain a vertex from the complete subgraph - but does it maximize the number of edges among all $k \cdot G$ -free graphs?

We discuss recent progress on this question; in particular, we show that the given construction is extremal for a large class of bipartite graphs, including those which have a vertex adjacent to all cycles. (Received September 20, 2015)