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Christopher L Kocs* (kocs@math.utah.edu). *Absolute Galois group computation.*

Given an odd integer n , there exists a surjective group homomorphism ϕ from $\text{Spin}_n(\mathbb{C})$ onto $\text{SO}_n(\mathbb{C})$, such that the following sequence is exact:

$$1 \longrightarrow \langle -1 \rangle \longrightarrow \text{Spin}_n(\mathbb{C}) \xrightarrow{\phi} \text{SO}_n(\mathbb{C}) \longrightarrow 1.$$

For any field extension F of \mathbb{Q}_2 , we construct a homomorphism $\psi : \text{Gal}(\bar{F}/F) \longrightarrow \text{SO}_n(\mathbb{C})$, and we consider when there is homomorphism $h : \text{Gal}(\bar{F}/F) \longrightarrow \text{Spin}_n(\mathbb{C})$ such that the below diagram

$$\begin{array}{ccc} & \text{Spin}_n(\mathbb{C}) & \\ & \nearrow h & \downarrow \phi \\ \text{Gal}(\bar{F}/F) & \xrightarrow{\psi} & \text{SO}_n(\mathbb{C}) \end{array}$$

commutes. This problem can be rephrased in terms of Clifford algebras and their corresponding quadratic forms. Ultimately, we are lead to compute the Hasse invariants, as a product of gauss sums, associated with these quadratic forms. (Received August 29, 2011)