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**Joseph Gubeladze\*** ([soso@sfsu.edu](mailto:soso@sfsu.edu)), Department of Mathematics, San Francisco State University, San Francisco, CA 94132. *Tautological part of  $K$ -theory of projective toric varieties*. Preliminary report.

For any functor  $F$  from (commutative) rings to abelian groups and a graded ring  $R = R_0 \oplus R_1 \oplus \cdots$  the group  $F(R_0)$  splits off from  $F(R)$ . The former can be viewed as the *tautological* part of the latter. Speaking geometrically, this is an essentially affine phenomenon. For a field  $k$ , how many copies of  $K_0(k) = \mathbf{Z}$  can one split off from the Grothendieck group  $K_0(X)$  of a projective toric variety  $X$  over  $k$ ? Using Thomason's localization technique and the fundamental theorem of  $K$ -theory, one devises an iterative process for splitting off many copies of  $K_0(k)$  from  $K_0(X)$ . The process unavoidably involves higher groups. It also goes through for all higher  $K$ -groups and general coefficient rings. Conjecturally, a  $K$ -group of a projective toric variety contains at least as many copies of the corresponding  $K$ -group of the base ring as the number of vertices of the underlying polytope, i. e., the number of standard affine toric charts. The case of a projective space shows that this is a sharp estimate. (Received August 27, 2011)