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**Timur Sadykov\*** ([sadykovtm@rsute.ru](mailto:sadykovtm@rsute.ru)), Russian State University, of Trade and Economics, Moscow, 125993, Russia. *On analytic complexity of special functions.*

The Kolmogorov-Arnold theorem yields a representation of a multivariate continuous function in terms of a composition of functions of at most two variables. In the analytic case, understanding the complexity of such a representation naturally leads to the notion of the analytic complexity of a bivariate (multi-valued) analytic function introduced and studied by V.K.Beloshapka (Russian J. Math. Phys. 14, no. 3, 2007, pp. 243-249.). According to Beloshapka's local definition, the order of complexity of any univariate function is equal to zero while the  $n$ -th complexity class is defined recursively to consist of functions of the form  $a(b(x, y) + c(x, y))$ , where  $a$  is a univariate analytic function and  $b$  and  $c$  belong to the  $(n - 1)$ -th complexity class. With such a hierarchy of complexity classes, one can associate a number of differential and algebraic invariants. A randomly chosen bivariate analytic function will most likely have infinite analytic complexity. However, for a number of important families of special functions their complexity is finite and can be computed or estimated. Using properties of solutions to the Hopf equation and the Gelfand-Kapranov-Zelevinsky system we obtain estimates for the analytic and polynomial complexity of such functions as well as plane webs. (Received August 28, 2011)