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Orbital stability of solitary waves of a 3-coupled nonlinear Schrödinger system.

In this talk, consideration is given to the 3-coupled nonlinear Schrödinger system

$$i\frac{\partial}{\partial t}u_j + \frac{\partial^2}{\partial x^2}u_j + \sum_{i=1}^3 b_{ij}|u_i|^2u_j = 0,$$

where u_j are complex-valued functions of $(x, t) \in \mathbb{R}^2$, $j = 1, 2, 3$, and b_{ij} are positive constants satisfying $b_{ij} = b_{ji}$. It will be shown first that if the symmetric matrix $B = (b_{ij})$ satisfies certain conditions, then ground-state solutions of the 3-coupled nonlinear Schrödinger system exist, and moreover, they are orbitally stable. The theory is then extended to include solitary waves as well. In particular, it will be shown that when a solitary wave is perturbed, the perturbed solution must stay close to a solitary-wave profile in which the translation and phase parameters are prescribed functions of time. Properties of these functions are then studied. This is a continuous work of our previous paper where the 2-coupled nonlinear Schrödinger system was considered. (Received August 22, 2011)