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**Michael Young\*** (myoung@iastate.edu) and **Lale Ozkahya**. *Anti-Ramsey number of matchings in hypergraphs.*

A  $k$ -matching in a hypergraph is a set of  $k$  edges such that no two of these edges intersect. The anti-Ramsey number of a  $k$ -matching in a complete  $s$ -uniform hypergraph,  $\mathcal{H}$ , on  $n$  vertices,  $ar(n, s, k)$ , is the smallest integer  $c$ , such that in any coloring of the edges of  $\mathcal{H}$  with exactly  $c$  colors,  $\mathcal{H}$  will contain a  $k$ -matching such that each edge of the matching has a distinct color. The Turán number,  $ex(n, s, k)$ , is the maximum number of edges in an  $s$ -uniform hypergraph on  $n$  vertices with no  $k$ -matching. It is known that for  $n > 2k$ ,  $ar(n, 2, k) = ex(n, 2, k - 1) + 2$  and for  $n = 2k$ ,

$$ar(n, 2, k) = \begin{cases} ex(n, 2, k - 1) + 2 & \text{if } k < 7 \\ ex(n, 2, k - 1) + 3 & \text{if } k \geq 7. \end{cases}$$

We conjecture, for  $k \geq 2$ , if  $n > sk$ ,  $ar(n, s, k) = ex(n, s, k - 1) + 2$  and if

$$n = sk, ar(n, s, k) = \begin{cases} ex(n, s, k - 1) + 2 & \text{if } k < c_s \\ ex(n, s, k - 1) + s + 1 & \text{if } k \geq c_s \end{cases},$$

where  $c_s$  is a constant dependent on  $s$ . We prove this conjecture

for  $k = 2, k = 3$ , and sufficiently large  $n$ , as well as provide upper and lower bounds. (Received August 19, 2011)