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**James Michael Wilson\*** (jmwilson@uvm.edu), 16 Colchester Avenue, Department of Mathematics, University of Vermont, Burlington, VT 05405. *Almost-orthogonality in weighted spaces.*

For  $\alpha > 0$ , let  $\mathcal{C}_\alpha$  be the uniformly (norm  $\leq 1$ )  $\alpha$ -Hölder continuous functions with supports contained in the unit ball of  $\mathbf{R}^d$ . Let  $\{\phi^{(Q)}\} \subset \mathcal{C}_\alpha$  be any family indexed over the dyadic cubes  $Q$ . If  $x_Q$  is the center of  $Q$  and  $\ell(Q)$  is its sidelength, define

$$\phi_{z_Q}^{(Q)}(x) \equiv \phi^{(Q)}(2(x - x_Q)/\ell(Q)),$$

which is  $\phi^{(Q)}$  translated and dilated (but not scaled) to the cube  $Q$ . We will show that if  $w$  is an  $A_\infty$  weight then the family  $\{\phi_{z_Q}^{(Q)}/|Q|^{1/2}\}$  is almost-orthogonal in  $L^2(dx)$  if and only if the family  $\{\phi_{z_Q}^{(Q)}/w(Q)^{1/2}\}$  is almost-orthogonal in  $L^2(w)$ ; where we say a family  $\{\psi_k\}$  is almost-orthogonal in  $L^2(\mu)$  if there is an  $R < \infty$  such that, for all finite linear sums  $\sum \lambda_k \psi_k$ ,

$$\int |\sum \lambda_k \psi_k|^2 d\mu \leq R \sum |\lambda_k|^2.$$

If time permits we will say something about how this relates to stability of almost-orthogonal expansions. (Received February 12, 2012)