

1081-57-209

**Alissa Crans** and **Jozef H. Przytycki\*** (przytyck@gwu.edu), Department of Mathematics, George Washington University, Washington, DC 20052, and **Krzysztof Putyra**. *Torsion in one term distributive homology*. Preliminary report.

Let  $(X; *)$  be a shelf, that is a magma with a right self-distributive operation  $((a * b) * c = (a * c) * (b * c))$ . We consider (one-term) distributive homology with a chain complex  $C_n(X) = ZX^{n+1}$  and the boundary operation given by  $\partial(x_0, x_1, \dots, x_n) = (x_1, \dots, x_n) + \sum_{i=1}^n (-1)^i (x_0 * x_i, \dots, x_{i-1} * x_i, x_{i+1}, \dots, x_n)$ . It was conjectured that such homology  $H_k^{(*)}(X)$  is always torsion free (for a rack it is known to be acyclic). We show here the opposite, the homology is reach in torsion. For example, we define  $(X_{n,k}; *)$ ,  $k < n$  with  $X_{n,k} = \{1, 2, \dots, n\}$  and  $i * j = j$  for  $i, j < n$  or  $j = n$ , furthermore  $n * i = i + 1$  for  $i < k < n$ , and  $n * i = 1$  for  $k \leq i < n$ , then,  $H_1^{(*)}(X_{n,k}) = Z^2 \oplus Z_k^{n-k-1}$ . This holds also for infinite  $n$ , producing infinite torsion. It is still an open problem whether left-connected  $(H_0(X) = Z)$  shelves can have torsion in homology. (Received February 11, 2012)