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Marina Dombrovskaya* (dombrom@math.wustl.edu). *Quotients of subgroup lattices of finite abelian p -groups.* Preliminary report.

Let G be a finite abelian p -group of type λ . It is well-known that the lattice $L_\lambda(p)$ of subgroups of G is the order-theoretic p -analogue of the chain product $[0, \lambda]$. However, any surjection $\varphi : L_\lambda(p) \rightarrow [0, \lambda]$ with order analogue properties does not respect group automorphisms. We are interested in $\overline{L_\lambda(p)}$, the quotient lattice of $L_\lambda(p)$ under the action of a Sylow p -subgroup of the automorphism group of G . This quotient lattice is particularly interesting since it respects group automorphisms, has the property that the size of an orbit of the action is a power of p , and is closely related to the product of chains $[0, \lambda]$. We will discuss combinatorial properties of $\overline{L_\lambda(p)}$ and several other interesting quotients of $L_\lambda(p)$ that arise as a consequence of studying $\overline{L_\lambda(p)}$. (Received January 02, 2012)