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For a property Γ and a family of sets \mathcal{F} , let $f(\mathcal{F}, \Gamma)$ be the size of the largest subfamily of \mathcal{F} having property Γ . For a positive integer m , let $f(m, \Gamma)$ be the minimum of $f(\mathcal{F}, \Gamma)$ over all families of size m . A family \mathcal{F} is said to be B_d -free if it has no subfamily $\mathcal{F}' = \{F_I : I \subseteq [d]\}$ of 2^d distinct sets such that for every $I, J \subseteq [d]$, both $F_I \cup F_J = F_{I \cup J}$ and $F_I \cap F_J = F_{I \cap J}$ hold. A family \mathcal{F} is a -union-free if $F_1 \cup \dots \cup F_a \neq F_{a+1}$ whenever F_1, \dots, F_{a+1} are distinct sets in \mathcal{F} . We verify a conjecture of Erdős and Shelah that $f(m, B_2\text{-free}) = \Theta(m^{2/3})$. We also obtain lower and upper bounds for $f(m, B_d\text{-free})$ and $f(m, a\text{-union free})$. (Received January 18, 2012)