Let \( G \) be a graph on \( n \) vertices with independence number two. We prove that \( G \) contains an odd clique minor of size at least \( \frac{n}{2} \) if \( G \) does not contain certain small graph as an induced subgraph. (Received January 17, 2012)