

1079-05-43

**Sarah Crown Rundell\*** (rundells@denison.edu), 100 West College St, Department of Mathematics, Denison University, Granville, OH 43023. *The coloring complex of a hypergraph.*

Let  $G$  be a graph with  $n$  vertices and at least one edge. The coloring complex  $\Delta(G)$  was defined by Steingrímsson, and is a simplicial complex that is associated to  $G$  whose  $r$ -faces consist of all ordered set partitions  $[B_1, \dots, B_{r+2}]$  of the vertices of  $G$  so that at least one of the  $B_i$  contains an edge of  $G$ . Jonsson showed that  $\Delta(G)$  is a constructible complex, and the rank of the unique nontrivial homology group is  $|\chi_G(-1)| - 1$ , where  $\chi_G(\lambda)$  denotes the chromatic polynomial of  $G$ . Let  $H$  be a hypergraph with  $n$  vertices. In this talk, we define the coloring complex of a hypergraph,  $\Delta(H)$ , and we will discuss its homology. In particular, in the case where the hypergraph is a complete  $k$ -uniform hypergraph,  $\Delta(H)$  is a shellable complex, and the rank of its unique nontrivial homology group can be expressed in terms of the chromatic polynomial of  $H$ . Using the Eulerian idempotents, one can place a decomposition on this nonzero homology group, and the rank of the  $j^{\text{th}}$  component in this decomposition equals the absolute value of the coefficient of  $\lambda^j$  in the chromatic polynomial of  $H$ . We also will discuss the homology of the cyclic coloring complex of a complete  $k$ -uniform hypergraph. (Received December 02, 2011)