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Given a finite group G and a number field k , a well-known conjecture asserts that the set $R_t(k, G)$ of Steinitz classes of tame G -Galois extensions of k is a subgroup of the ideal class group of k . In this paper we investigate an explicit candidate for $R_t(k, G)$, when G is of *odd* order. More precisely, we define a subgroup $\mathcal{W}(k, G)$ of the class group of k and we prove that $R_t(k, G) \subseteq \mathcal{W}(k, G)$. We show that equality holds for all groups of odd order for which a description of $R_t(k, G)$ is known so far. Furthermore, by refining techniques introduced in [?], we use the Shafarevich-Weil Theorem in cohomological class field theory, to construct some tame Galois extensions with given Steinitz class. In particular, this allows us to prove the equality $R_t(k, G) = \mathcal{W}(k, G)$ when G is a group of order dividing ℓ^4 , where ℓ is an odd prime. (Received December 14, 2011)