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**Lindsay N. Childs\*** (lchilds@albany.edu). *Fixed point free pairs of homomorphisms and Hopf Galois structures.*

Given finite groups  $\Gamma$  and  $G$  of order  $n$ , it is known that regular embeddings from  $\Gamma$  to the holomorph of  $G$  yield Hopf Galois structures on a Galois extension  $L|K$  of fields with Galois group  $\Gamma$  given by  $K$ -Hopf algebras  $H$  whose associated group is  $G$ . We consider regular embeddings that arise from fixed point free pairs of homomorphisms from  $\Gamma$  to  $G$ . When  $\Gamma$  and  $G$  are isomorphic and one homomorphism is the identity, then regular embeddings arise from fixed point free endomorphisms of  $G$ , an approach that, for example, yields all regular embeddings from  $S_n$  to  $Hol(S_n)$  for  $n > 6$ . If  $G$  is a complete group, then all regular embeddings from  $\Gamma$  to  $G$  arise from fixed point free pairs. We compute some examples. Kohl (1997) proved that if  $p$  is an odd prime and  $\Gamma$  is a cyclic group of order  $p^n$ , then every Hopf Galois structure on a Galois extension of fields with Galois group  $\Gamma$  has associated group  $\Gamma$ , and hence is abelian. Using fixed point free pairs, we prove that if  $p$  is an odd prime and  $\Gamma$  is a non-cyclic abelian  $p$ -group of order  $p^n$ ,  $n \geq 3$ , then  $L|K$  admits a non-abelian Hopf Galois structure. (Received January 11, 2012)