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Milano, Italy. *Spectral Triples on the Sierpinski gasket.*

The aim of the seminar is to reports on collaborations with D. Guido, T. Isola (Roma - University Tor Vergata) and J.L. Sauvageot (University Paris VII) show how to construct Dirac operators  $D$  and Spectral Triples  $(\mathcal{F}, D, H)$ , in the sense on A. Connes, on the Sierpinski gasket  $K$ , starting from the canonical Dirichlet form  $(\mathcal{E}, \mathcal{F})$  on it. We determine the whole dimensional spectrum showing also that the Hausdorff measure of  $K$  can be obtained as a residue at a pole  $d_D < 2$  of the analytic continuation of the volume-zeta functional of  $D$ . We also introduce a natural energy-zeta functional associated with  $D$  from which the Dirichlet form can be obtained as a residue at a pole  $\delta_D < 2$ . We finally study the Connes metric proving that the induced metric on  $K$  is bi-Lipschitz with respect to the Euclidean geodesic metric of  $K$ . As a last result we prove that the Fredholm module associated with  $D$  couples nontrivially with all generators of the  $K_1$ -theory group of the gasket. (Received June 29, 2011)